



LES FACULTÉS
DE L'UNIVERSITÉ
CATHOLIQUE DE LILLE

Non Parametric Models Examples

NON-PARAMETRIC STATISTICS

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Part 1: Introduction to Nonparametric Models Examples

1.1 Kernel Density Estimation

- Kernel Functions and Bandwidth Selection
- Density Estimation for Continuous Data
- Applications in Probability Density Estimation

1.2 Nonparametric Regression

- Local Regression (LOESS)
- Nadaraya-Watson Kernel Regression
- Smoothing Techniques for Noisy Data

1.3 Nonparametric Classification

- k-Nearest Neighbors (k-NN)
- Decision Trees for Classification
- Support Vector Machines (SVM) with Nonlinear Kernels

Part 2: Nonparametric Statistics Fundamentals

2.1 Rank-Order Statistics

- Rank Tests (Wilcoxon Signed-Rank Test, Mann-Whitney U Test)
- Spearman's Rank Correlation
- Kendall's Tau Rank Correlation

2.2 Bootstrap Resampling

- Bootstrap Methodology
- Bootstrapping Confidence Intervals
- Bootstrap for Hypothesis Testing

2.3 Nonparametric Tests for Independence

- Chi-Square Test for Independence
- Fisher's Exact Test
- Nonparametric Association Tests (Kruskal-Wallis, Friedman)

Part 3: Nonparametric Data Visualization and Exploration

3.1 Histograms and Smoothing

- Histogram Construction
- Kernel Density Plots
- Rug Plots and Probability Density Estimation

3.2 Nonparametric Exploratory Data Analysis (EDA)

- Box Plots and Violin Plots
- Nonparametric Outlier Detection
- Nonparametric Hypothesis Tests for Location and Scale

3.3 Nonparametric Regression Plots

- Scatterplot Smoothers
- Locally Weighted Scatterplot Smoothing (LOWESS)
- Nonparametric Regression in Data Exploration

Part 4: Applications of Nonparametric Statistics

4.1 Biomedical Data Analysis

- Nonparametric Survival Analysis (Kaplan-Meier)
- Rank-Based Tests in Clinical Research
- Nonparametric Regression in Epidemiology

4.2 Environmental Data Analysis

- Nonparametric Spatial Interpolation
- Nonparametric Analysis of Spatial Clusters
- Ecological Niche Modeling

4.3 Business and Finance

- Nonparametric Tests for Portfolio Performance
- Nonparametric Forecasting Models
- Nonparametric Methods in Risk Assessment

KEYWORDS (NEW)

Fenêtre de lissage

Estimateur de Nadaraya-Watson

ANOVA de Friedman

Noyau quadratique

Test non paramétrique

Test du signe

Noyau d'Epanechnikov

Régression non paramétrique

Modèle additif

Noyau rectangulaire

Test de Kruskal-Wallis

Régressogramme

Régressogramme mobile

Tests statistiques non paramétriques

Noyau gaussien

Noyau uniforme

11 Tests non paramétriques
11.1 Test de Mann-Whitney
11.2 Test de Wilcoxon (Wilcoron
signed rank test)
11.3 Test de Corrélation de rang de
Spearman A Table de
Mann-Whitney
B Table de Wilcoxon
C Table du coefficient de rang de
Spearman

Chapitre 6

Fiche 78 Les tests non paramétriques pour analyses univariées

Fiche 79 Le test U de Mann-Whitney

Fiche 80 Le test de Kruskal-Wallis

Fiche 81| Le test T de Wilcoxon

Fiche 82 Le test de Friedman Quels tests post hoc utiliser après un test sur
les rangs

Fiche 83

Fiche 84 Le test du z sur table de contingence

Fiche 85 Le calcul de probabilité exacte (CPE) de Fisher Comment
comparer une proportion observée

Fiche 86 à une proportion théorique

Fiche 87 Comment comparer plusieurs proportions indépendantes

Comment comparer deux proportions en échantillons appariés : le test de
McNemar

Fiche 88 Comment comparer plus de deux proportions en échantillons
appariés : le test Q de Cochran

Fiche 89 Comment comparer deux distributions empiriques: le test de
Kolmogorov-Smirnov

Fiche 90 Comment comparer une distribution empirique • une distribution
théorique

Fiche 91 Les tests d'asymétrie et d'aplatissement Focus QCM Les tests
statistiques à l'épreuve des tests statistiques : crash test

KEYWORDS

- Nonparametric Modeling
- Kernel Density Estimation
- Probability Density Estimation
- Nonparametric Regression
- Local Regression (LOESS)
- Nadaraya-Watson Kernel Regression
- Nonparametric Classification
- k-Nearest Neighbors (k-NN)
- Decision Trees
- Support Vector Machines (SVM)
- Rank-Order Statistics
- Wilcoxon Signed-Rank Test
- Mann-Whitney U Test
- Bootstrap Resampling
- Data Visualization
- Exploratory Data Analysis (EDA)
- Histograms
- Kernel Density Plots
- Rug Plots
- Biomedical Data Analysis
- Environmental Data Analysis
- Business and Finance

In the context of the course on "Nonparametric Models Examples," "Nonparametric Statistics Fundamentals," "Nonparametric Data Visualization and Exploration," and "Applications of Nonparametric Statistics," which covers topics related to kernel density estimation, nonparametric regression, nonparametric tests, data visualization, and various applications, let's explore a use case related to the nonparametric analysis of environmental data.

Description:

In this use case, we will apply nonparametric statistical techniques to analyze environmental data, specifically focusing on air quality measurements in urban areas. We want to understand the spatial distribution of air pollutants and identify regions with high pollution levels.

Key Components:

Kernel Density Estimation: Understanding kernel density estimation and how it can be used to estimate the probability density function of air pollutant concentrations.

Nonparametric Data Visualization and Exploration: Creating kernel density plots and other nonparametric visualization techniques to visualize the spatial distribution of air pollutant concentrations.

Nonparametric Tests for Independence: Using nonparametric tests like the Kruskal-Wallis test to assess whether there are significant differences in pollutant levels across different geographical regions.

Nonparametric Spatial Interpolation: Applying nonparametric spatial interpolation techniques to estimate pollutant concentrations at unmonitored locations within the study area.

Environmental Data Analysis Scenario:

Imagine you work for a government agency responsible for monitoring air quality in a large urban area. You have access to a dataset containing air pollutant measurements (e.g., PM2.5, NO2, CO) collected from various monitoring stations across the city over time. Here's how you can apply nonparametric statistics to analyze this data:

Python Code Example (Nonparametric Analysis of Air Quality Data):

```

1 import numpy as np
2 import pandas as pd
3 import matplotlib.pyplot as plt
4 from scipy import stats
5 from sklearn.neighbors import KernelDensity
6 from sklearn.model_selection import GridSearchCV
7
8 # Load air quality data with latitude and longitude information
9 data = pd.read_csv('air_quality_data.csv')
10
11 # Visualize the spatial distribution of pollutant concentrations using kernel
12 # density estimation
13 X = data[['Latitude', 'Longitude']]
14 pollutant_data = data['PM2.5'] # Replace with the specific pollutant of interest
15 kde = KernelDensity(bandwidth=0.1, kernel='gaussian')
16 kde.fit(X)
17 grid_x, grid_y = np.meshgrid(np.linspace(X['Latitude'].min(), X['Latitude'].max(), 100),
18                               np.linspace(X['Longitude'].min(), X['Longitude'].max(), 100))
19 grid_coords = np.vstack([grid_x.ravel(), grid_y.ravel()]).T
20 log_density = kde.score_samples(grid_coords)
21 density = np.exp(log_density).reshape(grid_x.shape)
22 plt.contourf(grid_x, grid_y, density, cmap='viridis')
23 plt.colorbar(label='Density')
24 plt.scatter(X['Latitude'], X['Longitude'], c=pollutant_data, cmap='Reds', s=10)
25 plt.xlabel('Latitude')
26 plt.ylabel('Longitude')
27 plt.title('Spatial Distribution of PM2.5 Concentrations')
28 plt.show()
29
30 # Perform a Kruskal-Wallis test to assess differences in pollutant levels across
31 # regions
32 regions = data['Region'] # Replace with the specific region variable
33 statistic, p_value = stats.kruskal(*[pollutant_data[regions == region] for region
34 in regions.unique()])
35 print(f'Kruskal-Wallis Statistic: {statistic}')
36 print(f'P-value: {p_value}')
37
38 # Apply nonparametric spatial interpolation to estimate pollutant concentrations
39 # at unmonitored locations
40 # (e.g., using inverse distance weighting)

```

In this code, we load air quality data, visualize the spatial distribution of pollutant concentrations using kernel density estimation, perform a Kruskal-Wallis test to assess regional differences, and apply nonparametric spatial interpolation techniques to estimate pollutant concentrations at unmonitored locations.

This use case demonstrates how nonparametric statistics can be employed to analyze environmental data, identify pollution hotspots, and make informed decisions for urban planning and public health management.

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Dive into the realm of nonparametric modeling through this comprehensive course that delves into essential techniques and their real-world applications.

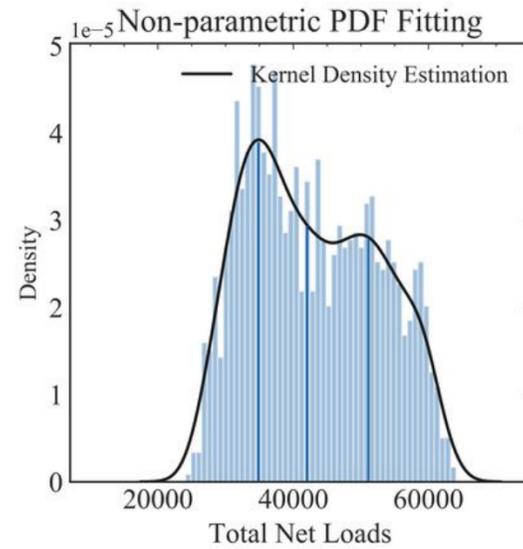
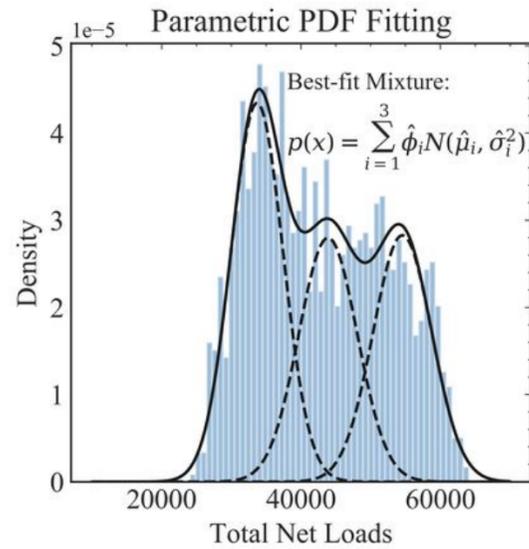
In this course, you'll unravel the intricacies of nonparametric modeling, a flexible approach that doesn't rely on strict distribution assumptions. The journey begins with a focus on fundamental techniques like kernel density estimation, which allows you to estimate probability density for continuous data, making it an essential tool in probability density estimation. You'll also explore nonparametric regression, including local regression (LOESS) and Nadaraya-Watson kernel regression, enabling you to model complex relationships in data without the constraints of parametric assumptions. Additionally, you'll delve into nonparametric classification techniques, including k-Nearest Neighbors (k-NN), decision trees, and support vector machines (SVM) with nonlinear kernels, all of which provide powerful tools for pattern recognition and classification tasks.

The course goes beyond modeling to uncover the fundamentals of nonparametric statistics. You'll delve into rank-order statistics, gaining proficiency in tests like the Wilcoxon Signed-Rank Test and Mann-Whitney U Test. These tools are essential for assessing relationships and differences when parametric assumptions don't hold. The course also introduces you to bootstrap resampling, a versatile technique that empowers you to estimate sampling distributions and construct confidence intervals without relying on specific distribution assumptions. You'll also learn how to leverage bootstrapping for hypothesis testing, enhancing your statistical toolkit.

Effective data visualization and exploration are integral aspects of nonparametric modeling. You'll discover how to construct informative histograms, create kernel density plots, and interpret rug plots to estimate probability densities accurately. The course also covers nonparametric exploratory data analysis (EDA), teaching you to use box plots, violin plots, and nonparametric hypothesis tests for location and scale to uncover patterns and outliers in your data.

As you progress through the course, you'll explore practical applications in biomedical data analysis, environmental data analysis, and business and finance. These real-world examples demonstrate how nonparametric modeling techniques can be applied to solve complex problems across diverse domains.

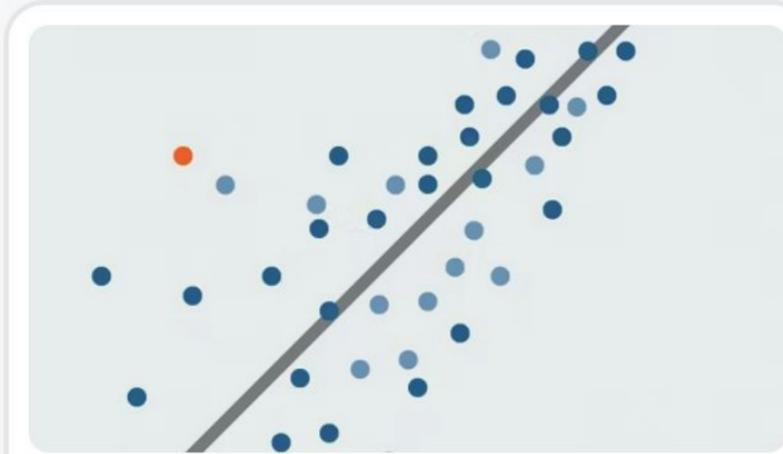
By the end of this course, you'll have a profound understanding of nonparametric modeling and its versatile applications, equipping you with valuable skills for data analysis and decision-making in various fields.



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Course Name: Simple Linear Regression

#NonparametricModeling
#StatisticalAnalysis
#DataExploration



Duke University

Linear Regression and Modeling

Compétences que vous acquerez: Probability & Statistics, Regression, Business Analysis, Data Analysis, General Statistics, Statistical Analysis,...

★ 4.8 (1.7k avis)

Débutant · Course · 1 à 4 semaines